Non-Destructive Evaluation of Green Ceramic Body Density by Ultrasonic Technique

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Introduction

The main quality requirements of manufactured ceramic tiles are established by International Organization for Standardization (ISO) standards for individual types of ceramic tiles [1]. Therefore the quality requirements of each line must correspond to ISO and other standards. The quality and durability of the tile depend directly on raw used materials, design of the production line, tile production process, installation and maintenance of the tiled surface [2].

One of very important parameters is density of a green ceramic tiles and particularly spatial variations of the density. The bulk density of a green ceramic body provides valuable information for tiles quality control in a final product inspection by determining porosity, impurities and cracks of the body [3, 4]. Currently, there are different ceramic products quality assurance methods, which allow evaluation of tile porosity, impurities and defects by analysis of the measured density [5-8].

The bulk density of a green ceramic body may be found by ultrasonic methods exploiting relationship between the density $\rho$ and velocity $c$ of ultrasonic waves. Analysis of the physical properties of the object under investigation may be performed by using longitudinal and/or transverse ultrasonic waves. Velocities of ultrasonic waves depend on elastic properties and density of the object under investigation.

The measurements of elastic properties have received much attention, therefore various techniques have been developed which allow perform static loading tests and dynamic ultrasonic and vibration resonant frequency measurements [4, 5].

The ultrasonic longitudinal wave velocity in an elastic homogeneous medium depends on the tested object density $\rho$, its Young’s modulus $E$ and the Poisson’s ratio $\nu$ and is given by [6]

$$c_L = \sqrt{\frac{E}{\rho} \cdot \frac{1-\nu}{(1+\nu)(1-2\nu)}}.$$  \hspace{1cm} (1)

Correspondingly, the velocity of an ultrasonic shear wave in an elastic homogeneous medium is [6]

$$c_T = \frac{E}{2\rho} \cdot \frac{1}{(1+\nu)}.$$  \hspace{1cm} (2)

From equation (1) follows that in order to determine from the measured longitudinal ultrasound wave velocity one material parameter, for example, the density $\rho$, others two parameters must be known or measured by other methods.

Equations (1) and (2) show that if both longitudinal and shear wave velocities can be measured, then the Young’s modulus and the Poisson’s ratio may be determined. However, in many quality control applications, such as evaluation of the density of a fired ceramic body from the measured longitudinal ultrasonic wave velocity, it is often assumed that the Poisson’s ratio can be treated as being approximately constant, and that the Young’s modulus follows a cubic relationship with density [7, 8]. As a result, the ultrasound velocity depends almost linearly on density.

These measurements are based on manual sampling of the flow of tiles by an operator who determines the apparent density of tiles. The use of such methods has enabled to control the production process of ceramic tiles on a discontinuous basis during last 20 years.

However, these measurements are very slow, complicated and they do not permit automatic control during a pressing operation. Further steps were directed to increase of a measurement speed, improvement of measurement repeatability and reduction of the measurement uncertainty. Currently, some manufacturers focus on a non-destructive estimation of the apparent density of green ceramic tiles. Example of such improvement is a measurement system, which is manufactured by Sonotec GmbH Halle and is based on an immersion method [9].

However, these systems measure the apparent density off-line and are more applicable for laboratory
measurements and selective production verification. In order to reduce the number of rejected tiles it is necessary to determine the bulk density of a green ceramic body online, since the spoiled green ceramic tiles will be detected before baking process. In this way it would be possible to reduce consumption of raw materials and to improve quality of the final product.

For such purpose the ultrasonic measuring system based on the air coupled ultrasonic approach has been developed [10]. This system has been applied for on-line apparent density measurements of ceramic tiles. However, stability and repeatability of the non-contact ultrasonic system may be affected by the following factors:
- Varying temperature (variation due to the drier);
- Dust;
- Vibrations;
- Humidity content of the tile;
- Superficial roughness of the tile;
- Movement of tiles.

For these reasons it is not feasible to reach the desired repeatability and accuracy using air-coupled ultrasonic technique.

Objective of this investigation was development of ultrasonic technique for evaluation of spatial variations of the green ceramic body density and experimental verification of this technique in laboratory conditions.

For solution of this problem measurements of ultrasonic longitudinal wave velocity were performed at different spatial points of green ceramic tiles by a direct transmission method. The obtained measurement results were analyzed and uncertainty of measurements was estimated.

**Measurement approach and preparation of specimens**

Evaluation of the measured apparent density \( \rho \) can be considered as a measurement of the two-dimensional field \( \rho(x, y) \) distributed in space, in our case in one plane, e.g. it is assumed that there no density variations across tiles thickness [11].

Physically measurements can be performed at discreet points \( x_i, y_j \) on both tile surfaces, what is equivalent to a spatial sampling of the field. In this case this field can be treated as a discreet apparent density field which is given by

\[
\rho(x_i, y_j) = \rho(i \cdot \Delta x, j \cdot \Delta y),
\]

where \( i \) and \( j \) is 0, 1,\ldots, \( N-1 \), \( N \) is number of measurements positions along \( x \) and \( y \) axis and \( \Delta x, \Delta y \) are spatial sampling intervals along the \( x \) and \( y \) axes.

From the measurements of the apparent density at the discreet points \( x_i, y_j \) the field \( \rho(x, y) \) is reconstructed and gives the bulk density distribution of a green ceramic body.

The original field \( \rho(x, y) \) can be restored by summing the measured discreet spatial field values at each field \( \rho(x_i, y_j) \) point multiplied by the interpolation function

\[
\rho(x, y) = \sum_{i,j} \rho(x_i, y_j) \frac{\sin(\omega_x \cdot (x-i \cdot \Delta x)) \sin(\omega_y \cdot (y-j \cdot \Delta y))}{(\omega_x \cdot (x-i \cdot \Delta x)) \cdot (\omega_y \cdot (y-j \cdot \Delta y))},
\]

where \( \omega_x \) and \( \omega_y \) are the highest spatial frequencies of the spatial frequency spectrum of the field \( \rho(x, y) \), which correspond to the field components with shortest periods.

In order this reconstruction would be accurate, the sampling intervals, or in other words, the distances between the measurement points must fulfill the following requirements

\[
\Delta x \leq \frac{\pi}{\omega_x} \text{ and } \Delta y \leq \frac{\pi}{\omega_y}.
\]

It is necessary to keep in mind that if the spatial spectrum is not band-limited, then additional measurement errors due to overlap of highest spatial components in the spatial spectrum may occur.

The main problem is that \textit{a priori} information about the apparent density field of green ceramic tiles is not yet available, therefore the spatial frequencies \( \omega_x \) and \( \omega_y \) are not known also. Therefore first of all measurements of ultrasound velocity at different points of green ceramic tile were carried out.

For this purpose 32 x 32 cm size green ceramic tiles, manufactured by AB „Dvarčionių keramika“, were selected. The tile was cut into 6x6 cm samples according to the Ultrasound Institute laboratory measuring platform (Fig. 1a). The samples were numbered and their thickness \( d_m \) values were measured. Numbering of the samples was used for reconstruction of the spatial distribution of the ceramic tiles density.

![Fig. 1.](image)

(a) by AB „Dvarčionių keramika“ made the 32 x 32 cm size green ceramic tile, (b) samples prepared for the density measurements, (c) for the ultrasonic wave propagation speed measurements direct transmission selected method

It is necessary to point out that in the case of a green ceramics, ultrasonic measurements may be performed only using a dry acoustic contact between ultrasonic transducers and the ceramic sample; otherwise the sample will be affected by a liquid, usually used for acoustic coupling. An additional problem is that one side of those specimens is with a rectangle pattern and therefore complicates establishment of a good quality dry acoustic contact. For solution of this problem a dry acoustic contact was realized up by means of a thin (0.73 mm ± 0.01 mm) vinyl film, which was inserted between the sample and ultrasonic
transducers. The acoustic contact between the film and ultrasonic transducers was obtained by glycerin.

According to results of previous experiments by various ultrasonic transducers for measurements were selected PISL CX-165 5 MHz .25''A and П111-5.0-K6-002 ultrasonic transducers, which were placed along one axis on both sides of the ceramic sample (Fig. 1b).

In order to obtain and ensure a stable acoustic contact for measurements, the ultrasonic transducers were pressed to the sample via a vinyl film by 4 kg weight. This weight was selected during experiments and was kept 2 min. until the measured waveform will be stable during each measurement on the sample, and the longitudinal ultrasonic wave propagation time measurement error was minimal for this film thickness variation.

**Measurements methods and results**

The objects under investigation are isotropic, therefore velocities of the ultrasonic longitudinal $c_L$ and transverse $c_T$ waves should not depend on a propagation direction. In this case the propagation velocity of longitudinal ultrasonic wave $c_L$ was measured in the center of the samples, when the transducers were placed on one axis from on both surfaces of the sample, using zero-crossing and cross-correlation techniques (Fig. 2).

![Fig. 2. The ultrasonic direct transmission density measurement technique set-up](image)

In order to compensate these errors it was proposed the following algorithm:

1. The segment of the signal up to the second measured zero-crossing point was selected using rectangular time window both in the reference signal and signal measured on sample:

$$u_{Ref,0}(t) = \begin{cases} u_{Ref}(t), & t \leq t_1, \\ 0, & \text{otherwise} \end{cases}, \quad (5)$$

$$u_{Tile,0}(t) = \begin{cases} u_{Tile}(t), & t \leq t_2, \\ 0, & \text{otherwise} \end{cases}, \quad (6)$$

2. The frequency spectrum of both of the segments were calculated using Fourier transform:

$$U_{Ref,0}(f) = \text{FT}[u_{Ref,0}(t)], \quad (7)$$

$$U_{Tile,0}(f) = \text{FT}[u_{Tile,0}(t)], \quad (8)$$

where FT denotes Fourier transform;

3. The frequency corresponding to the maximum of the spectrums were estimated:

$$f_{Ref,max} = \arg\max\{U_{Ref,0}(f)\}, \quad (9)$$

$$f_{Tile,max} = \arg\max\{U_{Tile,0}(f)\}; \quad (10)$$

4. The equivalent period of the signals were calculated:

$$T_{Ref} = 1/f_{Ref,max}, \quad (11)$$

$$T_{Tile} = 1/f_{Tile,max}; \quad (12)$$

5. Then the compensated propagation time in the sample of green ceramic tile can be estimated according

$$t_{Tile}^* = t_2^* - t_1^* - (T_{Tile} - T_{Ref}), \quad (13)$$

or

$$t_{Tile}^* = t_2^* - t_1^* - (T_{Tile} - T_{Ref})/2. \quad (14)$$

In order to estimate how efficient compensation is the reference signal is shown on Fig. 4 together with the signal

![Fig. 3. The reference signal (left) and the signal measured on the sample of green ceramic tile (right) with denoted measured zero-crossing time instances](image)
measured on the green ceramic tile, but shifted back according measured delay time. As can be seen best estimation time is obtained using second measured zero-crossing time instance and Eq. (13).

Then the longitudinal ultrasound velocity was calculated as

$$c_{\text{zc}} = \frac{d_m}{t_{\text{Tile}}}, \tag{15}$$

where \(d_m\) is the measured sample thickness at the measurement point.

![Fig. 4. Measured ultrasonic signals: 1- the reference signal, 2 - signal obtained on the sample; but shifted back in time domain using the delay time estimated according Eq. (14); 3 - signal obtained on the sample, but shifted back in time domain using the delay time estimated according Eq. (13); 4 - signal obtained on the sample, but shifted back in time domain using the delay time estimated using cross-correlation technique.](Image)

It is necessary to point out that method based on zero-crossing is susceptible to noise, therefore for measurements we also applied method based on a cross-correlation.

Cross-correlation technique is most reliable and accurate and is based on calculation of a cross-correlation function between the reference and the measured signal. In this case, the reference signal is the same as using the zero-crossing technique.

Using the cross-correlation technique the ultrasonic wave propagation speed was calculated in the following steps. The cross-correlation function \(y_{\text{cc}}(t)\) between the signal \(u_{\text{Ref}}(t)\) and \(u_{\text{Tile}}(t)\) is given by \([12]\)

$$y_{\text{cc}}(t) = \frac{1}{T} \int_0^T u_{\text{Tile}}(t) \cdot u_{\text{Ref}}(t - \tau) \, d\tau, \tag{16}$$

where \(\tau\) is the integration variable, \(T\) is total duration of the recorded signal (1–5 \(\mu\)s).

Determination of the maximum of the cross-correlation function \([13–15]\) \(t_{\text{cc}}\) corresponding to the time delay between the signals \(u_{\text{Ref}}(t)\) and \(u_{\text{Tile}}(t)\) is performed in the following way \([12]\)

$$t_{\text{cc}} = \arg \{\max[y_{\text{cc}}(t)]\}. \tag{17}$$

Then longitudinal ultrasound velocity was calculated as

$$c_{\text{cc}} = \frac{d_m}{t_{\text{cc}}}, \tag{18}$$

As can be seen in Fig. 4 the delay time estimation using this technique leads to the systematic error caused by attenuation. On the other hand the additional filtering of the reference signal can be used in order to reduce errors. However for that the attenuation dependency on frequency should be known, what is not determined strictly and can be different for samples of different ceramics.

The measurements were carried out at the ambient temperature \(T\) (\(T = 20.4 \degree C\)) and humidity \(\theta\) (\(\theta = 50 \%\)). In fact, humidity content of the object also affects the propagation speed of ultrasound, but its influence is not significant, because measurements are made with dried tiles at the constant humidity level (4 - 5) %.

Usually temperature and humidity of the manufacturing environment are not measured on-line, hence, in the case of on-line measurements an additional uncertainty occurs. If the influence of temperature \(T\) and humidity \(\theta\) are taken into account, the longitudinal ultrasound velocity \(c_L\) is given by \([16]\)

$$c_L(T, \theta) = \left( c + 0.59T \left( 1 + 0.004 \frac{\theta}{100} \right) \right). \tag{19}$$

In our case velocity values \((c_{\text{zc}}\) and \(c_{\text{cc}}\) are calculated using Eq. (15) and Eq. (18). The uncertainty of these measurements is calculated from the measurement results by evaluating all factors which affect the measurement of \(c_{\text{zc}}\) and \(c_{\text{cc}}\)

$$u_c = \sqrt{\left( \frac{W^2}{d_m} \cdot u_{d_m} \right)^2 + \left( \frac{W^2}{t_{\text{Tile}}^2} \cdot u_{t_{\text{Tile}}} \right)^2}, \tag{20}$$

where \(u_{t_{\text{Tile}}} = f\{f_f, \Delta f, \text{SNR, } AC\}\) is the measurement uncertainty of ultrasound propagation time, \(f_f\) is the signal frequency, \(\Delta f\) is the ADC time sampling step, SNR is the signal to noise ratio and \(AC\) estimates stability of the dry acoustic contact.

For example the ultrasound velocity \(c_{\text{zc}}\) and \(c_{\text{cc}}\) calculated the tile density \(\rho\) and the uncertainty \(u_c\) and \(u_{uc}\) in the sample 1 (Fig. 5) were measured as follows.

First of all the sample thickness was measured by a micrometer \((d_m = 8.19 \text{ mm} \pm 0.01 \text{ mm})\) and then the longitudinal ultrasound wave propagation times \(t_{\text{Tile}} = 5.6 \mu\text{s} \pm 12.0 \text{ ns}\) and \(t_{\text{cc}} = 6.1 \mu\text{s} \pm 15.0 \text{ ns}\) were measured by using the computerized measuring system.

![Fig. 5. Green ceramic sample (dimensions are given in mm) and the measuring point of the longitudinal ultrasonic wave propagation time \(t_m\).](Image)
Finally, the velocity of longitudinal ultrasonic waves was calculated using Eq. (15) and Eq. (18), with gives a systematic error of 112 m/s. From the obtained \( c_{zc} \) and \( c_{cc} \) measurements results their uncertainty were estimated:

\[
\begin{align*}
\nu_{zc} &= \sqrt{\frac{u_d^2}{u_{Tile}^2}} = 3 \text{ m/s}, \\
\nu_{cc} &= \sqrt{\frac{u_d^2}{u_{Tile}^2}} = 4 \text{ m/s}.
\end{align*}
\]

So, the velocity of longitudinal ultrasonic waves:

\[
\begin{align*}
c_{zc} &= \frac{d_m}{t_{Tile}} = 1463 \pm 6 \text{ m/s}, \\
c_{cc} &= \frac{d_m}{t_{cc}} = 1455 \pm 8 \text{ m/s}.
\end{align*}
\]

Then, a small rectangle test samples \((s_1, s_2, s_3, s_4)\) were cut out from this tile to determined relationship between obtained \( c_{zc} \) and \( c_{cc} \) values and the density. Subsequently they were weighed, measured its size, and calculated their density. Then was measured the ultrasonic wave propagation velocity in the middle of these samples. Obtained data presented in Table 1.

![Fig. 6. Spatial variations of the ultrasound velocity \( c_{zc} \) measured across a green ceramic tile](image-url)

![Fig. 7. Spatial variations of the density \( \rho \) of green ceramic tile](image-url)

### Table 1. Analysis results of tested samples

<table>
<thead>
<tr>
<th>Sample</th>
<th>( c_{zc}, \text{ m/s} )</th>
<th>( c_{cc}, \text{ m/s} )</th>
<th>( \rho, \text{ kg/m}^3 )</th>
</tr>
</thead>
<tbody>
<tr>
<td>s1</td>
<td>1461</td>
<td>1457</td>
<td>1860</td>
</tr>
<tr>
<td>s2</td>
<td>1463</td>
<td>1458</td>
<td>1863</td>
</tr>
<tr>
<td>s3</td>
<td>1470</td>
<td>1461</td>
<td>1869</td>
</tr>
<tr>
<td>s4</td>
<td>1470</td>
<td>1463</td>
<td>1871</td>
</tr>
</tbody>
</table>

So, the linear relationship between the tested sample density and the ultrasonic wave propagation velocity in the samples were determined using approximation. Exploiting this relationship the density of a sample \((1)\) was calculated for two cases \((c_{zc} \text{ and } c_{cc})\):

\[
\begin{align*}
\rho' (c_{zc}) &= 1.066c_{zc} + 303.4 = 1863 \text{ kg/m}^3 \pm 6\text{ kg/m}^3, \\
\rho'' (c_{cc}) &= 1.606c_{cc} - 478.9 = 1858 \text{ kg/m}^3 \pm 8\text{ kg/m}^3.
\end{align*}
\]

The uncertainty of the longitudinal ultrasound wave propagation speed measurement was changed to the uncertainty of a sample density measurement, because the apparent density \( \rho \) was calculated by exploiting relationship with the ultrasonic propagation velocity.

From the ultrasonic longitudinal wave velocity measurements, performed at different points according to Fig. 1b, two-dimensional spatial distribution of the velocity \( c_{l}(x,y) \) was obtained (Fig. 6). Correspondingly, using the procedure described above, two-dimensional spatial distribution of the density \( \rho(x,y) \) was calculated. Intermediate values between measurement points were obtained by interpolation (Eq. (4)).

From the results presented follows that the longitudinal wave velocity and, correspondingly, the density of green ceramic tiles depend on spatial coordinates in-plane of tiles. These spatial variations may influence quality of tiles, because after baking procedure they may cause deformation of tiles.

1. For quality monitoring of ceramic tiles during manufacturing process, estimation of the density spatial variations, based on measurement of the ultrasonic longitudinal wave velocity, may be efficiently used.
2. The longitudinal ultrasonic wave velocity may be measured by using zero-crossing and/or cross-correlation techniques.
3. In the case of the high signal to noise ratio and stable amplitude of the received ultrasonic signals the zero-crossing technique is more preferable than the cross-correlation technique as a simpler one. However it was found that by using the zero-crossing technique and performing measurements at different zero-crossings some systematic error occurs. For example, when the ultrasonic wave propagation time \( t_{zc} \) is measured between full signals period and between half signals period, the obtained \( c_{zc} \) values are correspondingly 1463 m/s and 1452 m/s, e.g., there is difference \( \sim 11 \) m/s in all measured cases. This difference may be eliminated by an appropriate calibration procedure.
4. The spatial distribution of the thickness $d_{\text{m}}$ was measured by a micrometer and this uncertainty is highest of all uncertainties. The average thickness deviation across the whole tile is $\sim 2.5 \, \mu\text{m}$.

5. Experimental verification of this technique carried out in laboratory conditions shows that it is necessary to perform more detailed the measurements of various tiles in order to determine optimal number of measurement points, which is enough for a reliable reconstruction of spatial distribution of a green ceramic density.

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References


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Laboratory measurements of spatial density distribution in green ceramic tiles were implemented using ultrasonic contact coupling measurement method. The main objective of these measurements is to measure spatial density distribution in pressed green ceramic tiles. Measurements of longitudinal ultrasonic wave propagation velocity were carried out using pulse and correlation methods and the tile density values were calculated. Evaluation of the measurement method, estimation of uncertainty of measurements and analysis of further improvements purposed to adapt it for on-line measurements in a production process were carried out. Ill. 7, bibl. 16, tabl. 1 (in English; abstracts in English and Lithuanian).


Presuotų keraminų plytelų ruošinių tankio erdviniams pasiskirstymui matuoti laboratorinėmis sąlygomis taikytas ultragarasinis tiesioginio kontaktu matavimo metodas. Svarbiausias šių matavimų uždavinys – nustatyti visų presuotų keraminų plytelų ruošinių tankio erdvini pasiskirstymą. Eksperimentų metu išlįginiai ultragarso bangų sklidimo greičio matavimai atlikti taikant impulsinių ir koreliacinių metodų, o plytelės tankio vertės apskaičiuotos įnaudojant ryši tarp ultragarso greičio ir plytelės tankio. Matavimų rezultatams įvertinti apskaičiuotos neapibrėžtys, įvertintas pats matavimo metodas ir numatyta, kaip jį toliau tobulinti ir pritaikyti matavimams gamybos linijoje. Ill. 7, bibl. 16, lent. 1 (anglų kalba; santraukos anglų ir lietuvių k.).